

Dalton Classes

pH & Buffer

- **Ionic Product of Water (K_w):**

Water is weak electrolyte.



$$K = \frac{[H^+][OH^-]}{[H_2O]} \approx \text{const as } H_2O \text{ is weak electrolyte}$$

So $K \cdot [H_2O] = \text{new const} = [H^+][OH^-]$

This new const is ionic product (K_w) of water.

$$\text{i.e. } K_w = [H^+][OH^-]$$

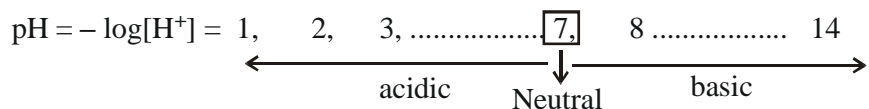
The product of $[H^+]$ & $[OH^-]$ is constant at a particular temperature and it is called ionic product of water.

$K_w = 10^{-14}$ at 25°C ; K_w changes only with temp.

- To convert $[H^+]$ of fractional data i.e. 10^{-1} (M) to 10^{-14} (M) into the integral values, \ominus ve logarithmic operation is done on the fractional (dilute) molar concentration of H^+ ions.
- \ominus ve logarithm is designated as "p". pH is an abbreviation for "power of hydrogen" where "p" is short form the German word for power, *potenz* and H is the element symbol for hydrogen.

$$-\log [H^+] = \text{pH}$$

- $[H^+]$ is molarity : $10^{-1}, 10^{-2}, 10^{-3} \dots\dots\dots 10^{-7}, 10^{-8} \dots\dots\dots 10^{-14}$ M



This pH scale is only at 25°C

- $K_w = [H^+][OH^-]$

$$-\log K_w = -\log [H^+] - \log [OH^-]$$

$$\text{p}K_w = \text{pH} + \text{pOH} = 14 \quad [\text{p}K_w = -\log 10^{-14} = 14]$$

i.e $\text{pH} = \text{pOH} = 7$ for water

- **Is it possible to have (-)ve pH of any solution?**

Ans. pH scale is used to convert fractional dilute concentrations into integral values but if it is applied on integral concentration, then pH may be \ominus ve or zero also

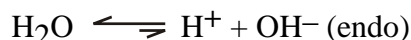
$$\text{pH of } 2 \text{ (M) HCl} \Rightarrow -\log 2 = \ominus \text{ve}$$

$$1 \text{ (M) HCl} \Rightarrow -\log 1 = 0$$

- **pH of boiled water < 7 is it acidic ?**

i) $\text{pH} < 7$ acidic ; $\text{pH} > 7$ alkaline & $\text{pH} = 7$ neutral - this scale is only at 25°C temp. So for boiled water i.e at 100°C temp. This scale is changed i.e. < 7 or > 7 pH may be neutral.

ii) $H^+ + OH^- \rightarrow H_2O$ - This acid-base neutralization reaction is always **exothermic** so dissociation of water into H^+ & OH^- must be **endothermic** in nature.



So under hot / boiled condition forward rate i.e. ionization of H_2O increases, so $[\text{H}^+]$ increases i.e. pH decreases but at the same time $[\text{OH}^-]$ also increases in the same ratio so it remains neutral.

● **pH of ice > 7 - is it alkaline ?**

same type answer

● **Calculation of pH of dilute mono basic strong acid.**

Ex. $10^{-2}(\text{N}) \text{HCl}$, $10^{-2}(\text{N}) \text{HCl} \equiv 10^{-2}(\text{M})$

As HCl is strong acid, $[\text{HCl}] = [\text{H}^+] = [\text{Cl}^-]$

i.e. $[\text{H}^+] = 10^{-2}(\text{M})$

$$\text{pH} = -\log [\text{H}^+] = -\log 10^{-2} = 2$$

● **Calculation of pH of dilute poly basic strong acid.**

Ex. $10^{-2}(\text{N}) \text{H}_2\text{SO}_4$

$$10^{-2}(\text{N}) \text{H}_2\text{SO}_4 = \frac{10^{-2}}{\text{basicity}} = \frac{10^{-2}}{2}(\text{M}) \text{H}_2\text{SO}_4$$

$$[\text{H}^+] = 2 \times \frac{10^{-2}}{2} = 10^{-2}(\text{M})$$

$$\therefore \text{pH} = 2$$

● **Calculation of pH of dilute mono acidic strong alkali**

Ex $10^{-2}(\text{N}) \text{NaOH}$

$$10^{-2}(\text{N}) \text{NaOH} \equiv 10^{-2}(\text{M}) \text{NaOH}$$

$$[\text{OH}^-] = 10^{-2}(\text{M})$$

$$\text{So, pOH} = -\log 10^{-2} = 2$$

$$\text{Again pH} + \text{pOH} = 14$$

$$\text{So, pH} = 14 - \text{pOH} = 14 - 2 = 12$$

● **Calculation of pH of dilute weak acid**

Ex $10^{-2}(\text{N}) \text{CH}_3\text{COOH}$ (20% dissociated)



c = molar concentration

$$c(1 - \alpha) \quad c\alpha \quad c\alpha$$

α = degree of dissociation.

$$[\text{H}^+] = c\alpha = 10^{-2} \times \frac{20}{100}$$

$$\text{pH} = -\log (10^{-2} \times 0.2) = 2 - \log 0.2$$

Ex $10^{-2}(\text{N}) \text{CH}_3\text{COOH}$ ($\text{pK}_a = 4.76$)



c = concentration of acid

$$c(1 - \alpha) \quad c\alpha \quad c\alpha$$

α = degree of ionization for 1 mole HA

$$\text{K}_a = \frac{[\text{H}^+][\text{A}^-]}{[\text{HA}]} = \frac{c\alpha \cdot c\alpha}{c(1 - \alpha)} = \frac{c\alpha^2}{1 - \alpha} \approx c\alpha^2 \quad \alpha \ll 1$$

$$\alpha = \sqrt{\frac{\text{K}_a}{c}} \quad \dots (i)$$

$$1 - \alpha \approx 1$$

$$[\text{H}^+] = c\alpha = c\sqrt{\frac{\text{K}_a}{c}} = \sqrt{\text{K}_a \cdot c}$$

$$\text{pH} = -\log \sqrt{K_a \cdot c} = -\frac{1}{2} \log K_a - \frac{1}{2} \log c$$

$$\boxed{\text{pH} = \frac{1}{2} \text{p}K_a - \frac{1}{2} \log c}$$

$$\begin{aligned} \text{pH} &= \frac{1}{2} \times 4.76 - \frac{1}{2} \log 10^{-2} \\ &= \left(\frac{4.76}{2} + \frac{2}{2} \right) = 1 + \frac{4.76}{2} \end{aligned}$$

● **Calculation pH of very dilute acid / alkali**

Ex $10^{-8}(\text{N}) \text{HCl}$

It is too dilute, so $[\text{H}^+]$ from water should not be neglected

$$\begin{aligned} [\text{H}^+]_{\text{t}} &= [\text{H}^+]_{\text{a}} + [\text{H}^+]_{\text{w}} \\ &= 10^{-8} + 10^{-7} \\ &= 10^{-7} (10^{-1} + 1) = 1.1 \times 10^{-7} \\ \text{pH} &= -\log (10^{-7} \times 1.1) = 7 - \log 1.1 \approx 6.96 \end{aligned}$$

Ex $10^{-8}(\text{N}) \text{NaOH} \equiv 10^{-8}(\text{M}) \text{NaOH}$

It is too dilute, so $[\text{H}^+]$ from water should not be neglected

$$\begin{aligned} [\text{OH}^-]_{\text{t}} &= [\text{OH}^-]_{\text{b}} + [\text{OH}^-]_{\text{w}} \\ &= (10^{-8} + 10^{-7}) = 10^{-7} (1.1) \\ \text{pOH} &= 7 - \log 1.1 = 6.96 \\ \therefore \text{pH} &= 14 - 6.96 = 7.04 \end{aligned}$$

Mixing Problems:

Q. Calculate the pH value of a solution obtained by mixing 50 ml of 0.2 (N) HCl with 50 ml of 0.1 (N) NaOH.

Ans. 50 ml 0.2 (N) HCl $\equiv (50 \times 0.2) = 10 \text{ ml } 1 (\text{N})$ acid
 50 ml 0.1 (N) NaOH $(50 \times 0.1) = 5 \text{ ml } 1 (\text{N})$ base
 So after mixing 5 ml 1 (M) acid remains in excess.
 Total volume = 50 + 50 = 100 ml
 \therefore New resulting solution: 100 ml S (N) $\equiv 5 \text{ ml } 1 (\text{N})$ acid
 $\therefore S = \frac{5 \times 1}{100} = \frac{1}{20} (\text{N})$ acidic reaction
 So, $\text{pH} = -\log \frac{1}{20} = -\log 0.05 = 1.30$

Q. What will be the pH of a solution obtained by mixing 800 ml of 0.05 (N) NaOH and 200 ml of 0.1 (N) HCl.

Ans. 800 ml 0.05 (N) NaOH $\equiv (800 \times 0.05) = 40 \text{ ml } 1 (\text{N})$ base
 200 ml 0.1 (N) HCl $\equiv (200 \times 0.1) = 20 \text{ ml } 1 (\text{N})$ acid
 i.e after mixing $(40 - 20) = 20 \text{ cc } 1 (\text{M})$ base is in excess.
 But total volume = $(800 + 200) = 1000 \text{ ml}$
 $\therefore 1000 \times S_{\text{final}} = 20 \times 1 (\text{N})$
 $S_{\text{f}} = \frac{20}{1000} = \frac{1}{50} (\text{N}) = 0.02 (\text{N})$
 So $\text{pOH} = -\log 0.02$ i.e $\text{pH} = 14 - \text{pOH} = (14 + \log 0.02) = 12.3$

Q. How many moles of Ca(OH)_2 must be dissolved to produce 250 ml. of an aqueous solution of pH = 10.65 ?

Ans. pH = 10.65 so pOH = 14 – 10.65 = 3.35

$$[\text{OH}^-]_{\text{solution}} = 10^{-3.35} = 10^{-14} \times 100.65$$

$$= 10^{-4} \times 4.466$$

$$= 4.466 \times 10^{-4} \text{ (M)}$$

One molecule of Ca(OH)_2 produces 2 OH^- ions

i.e. 1000 C.C. solution needs $2.235 \times 10^{-4} \text{ (M)}$ Ca(OH)_2 to produce pH = 10.65

$$250 \text{ C.C. solution needs } \frac{2.235}{4} \times 10^{-4} = 5.58 \times 10^{-5} \text{ moles}$$

Q. The pH of 0.1 (M) HCN is 5.2. Calculate its K_a

$$\text{Ans. pH} = \frac{1}{2} \text{p}K_a - \frac{1}{2} \log c \quad 2 \times \text{pH} = \text{p}K_a - \log c$$

$$5.2 = \frac{1}{2} \text{p}K_a - \frac{1}{2} \log 10^{-1}$$

$$5.2 \times 2 = \text{p}K_a + 1$$

$$\text{p}K_a = 10.4 - 1 = 9.4 ; \quad -\log K_a = 9.4$$

$$K_a = \text{anti log } (-9.4) \quad \log K_a = -9.4$$

$$K_a = 3.98 \times 10^{-10}$$

Q. What is the $[\text{H}^+]$ of 0.1 (N) CH_3COOH ? Calculate pH ? $K_a = 1.8 \times 10^{-5}$

$$\text{Ans. } \alpha = \sqrt{\frac{K_a}{c}} = \sqrt{\frac{1.8 \times 10^{-5}}{0.1}}$$

$$[\text{H}^+] = c\alpha = \sqrt{K_a \cdot c} = \sqrt{1.8 \times 10^{-5} \times 0.1}$$

$$= \sqrt{1.8 \times 10^{-6}}$$

$$= 1.34 \times 10^{-3} \text{ M}$$

$$\text{pH} = -\log (1.34 \times 10^{-3}) = 3 - \log 1.34$$

$$= 2.87$$

Q. 10 C.C. 10^{-2} (N) HCl is titrated by 10^{-2} (N) NaOH. Calculate pH at the following stages :

i) Before adding alkali

ii) 2 C.C. alkali is added

iii) 5 C.C. alkali is added

iv) 9 C.C. alkali is added

v) 9.9 C.C. alkali is added

vi) 10.0 C.C. alkali is added

vii) 10.1 C.C. alkali is added

Draw a plot of pH vs. volume of alkali & extend the idea for all sorts of acid-base titration & comment on the choice of indicator.

Ans. i) **Before adding alkali:**

$$10^{-2} \text{ (N) HCl} \equiv 10^{-2} \text{ (M) HCl} \equiv 10^{-2} \text{ (M) H}^{\oplus} \text{ [strong acid]}$$

$$\therefore \text{pH} = -\log 10^{-2} = 2$$

ii) **2 C.C. alkali is added:**

$$2 \text{ c.c. } 10^{-2} \text{ (N) NaOH consumes } 2 \text{ c.c. } 10^{-2} \text{ (N) HCl}$$

$$\text{Remaining acid} = 8 \text{ c.c. } 10^{-2} \text{ (N) HCl}$$

As the salt so formed is NaCl (SA + SB) it cannot change the pH of the medium so pH is due to HCl only

$$[\text{Acid}] = \frac{8 \times 10^{-2}}{12} \rightarrow \text{Total volume}$$

$$\begin{aligned} \text{pH} &= -\log (\text{H}^+) = -\log \frac{8 \times 10^{-2}}{12} \\ &= 2 - \log \frac{2}{3} = 2.176 \end{aligned}$$

iii) **5 C.C. NaOH is added:**

$$\text{pH} = -\log \frac{5 \times 10^{-2}}{15} = 2.477$$

iv) **9 C.C. NaOH is added :**

$$\text{pH} = -\log \frac{1 \times 10^{-2}}{19} = 3.278$$

v) **9.9 C.C. NaOH is added :**

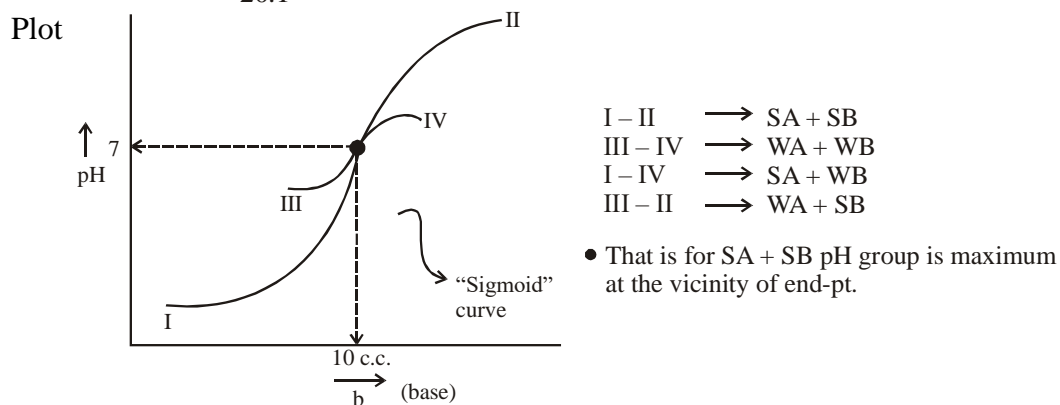
$$\text{pH} = -\log \frac{0.1 \times 10^{-2}}{19.9} = 4.298$$

vi) **10 C.C. NaOH is added :**

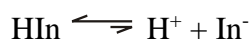
pH = 7 as total salt is NaCl which is salt of strong acid & strong base i.e. pH = 7

vii) **10.1 C.C. NaOH is added :**

$$\text{pH} = 14 + \log \frac{0.1 \times 10^{-2}}{20.1} = 9.696$$



Indicators are generally organic weak acids or base. Say, consider it is HIn. It ionizes as:



$$K_{\text{In}} = \frac{[\text{H}^+][\text{In}^-]}{[\text{HIn}]}$$

$$-\log K_{\text{In}} = -\log [\text{H}^+] - \log \frac{[\text{In}^-]}{[\text{HIn}]}$$

$$\text{p}K_{\text{In}} = \text{pH} - \log \frac{[\text{In}^-]}{[\text{HIn}]}$$

$$\text{pH} = \text{p}K_{\text{In}} + \log \frac{[\text{In}^-]}{[\text{HIn}]}$$

Those indicators are accepted where the colour of molecular form and that of ionic form are different.

There is a sensitivity factor for human eye to detect the change in colour over another. The concentration difference should be at least 10 times different to detect the change in colour.

If $[\text{In}^-] / [\text{HIn}] = 10 \rightarrow$ Colour of In^- is detected.

If $[\text{In}^-] / [\text{HIn}] = 1/10 \rightarrow$ Colour of HIn is detected.

So, to detect the visual change in colour by human eye the range of pH of an indicator will be

$$\text{pH} = \text{pK}_{\text{In}} \pm \log 10$$

$$\text{pH} = \text{pK}_{\text{In}} \pm 1$$

If this range of pH resides within the range of pH at the vicinity of end point of titration, that indicator is chosen for that titration.

So, for SA-SB titration → any kind of indicator can be used because range of pH at the vicinity of end point is maximum.

For SA-WB titration → Indicator which ionizes in acid medium can be used like methyl orange.

For WA-SB titration → Indicator which ionizes in basic medium can be used like phenolphthalein

For WA-WB titration → No suitable Indicator is found.

Buffer Solution

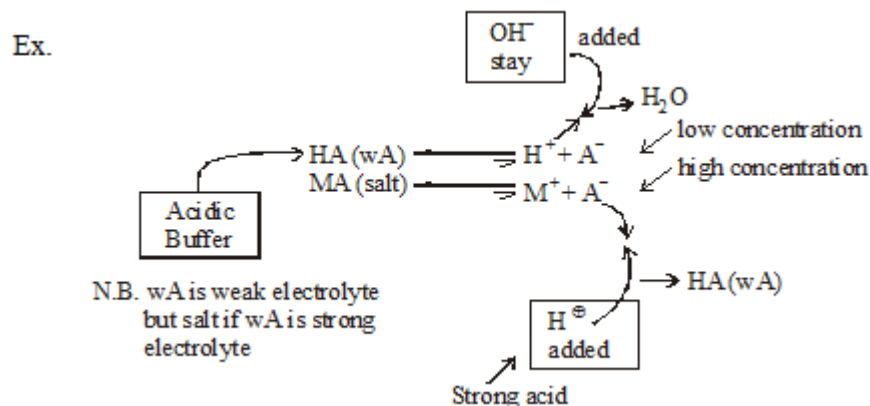
Definition : A mixture of weak acid & its salt or weak base & its salt which can resist the change in pH by adding a little amount of acid or alkali is called acidic or alkaline buffer respectively.

Ex. CH_3COOH (WA) + CH_3COONa → acidic buffer

NH_4OH (WB) + NH_4Cl → basic buffer

● Buffer action:

The mechanism by which a solution can resist the change in pH is called buffer action of that buffer.



- I. After adding a few drop of S.A. it is internally converted into W.A. i.e. lowering of pH is not significant.
 - II. After adding a few drops of S.B it reacts with H^+ from HA (WA) to form equivalent amount of H_2O (neutral). i.e. to compensate the loss of $[\text{H}^+]$ molecular HA further ionizes i.e $[\text{HA}]$ reduces & again as H_2O is formed total volume also increases i.e. $[\text{MA}]$ also decreases.
- i.e. $\frac{[\text{MA}]}{[\text{HA}]}$ ratio remains almost unaltered.
- i.e. $\text{pH} = \text{pK}_a + \log \frac{[\text{Salt}]}{[\text{Acid}]}$ equation tells us pH remains almost const.
- ⇒ the above two explanations tells us acidic buffer is a best buffer towards alkali and acidic buffer exhibits bad bufferial action towards acid.

● Buffer Capacity:

Definition: The amount of base (b) added to create unit change of pH is called buffer capacity (β) of that buffer.

$$\text{So, } \beta = \frac{db}{d(\text{pH})}$$

Say, $d(\text{pH}) = 1$; $\beta = db$

Say, a cc S(N) weak acid is added with b c.c. S(N) strong base & $a > b$.

$$[\text{Salt}] = \frac{b \times s}{(a+b)}; [\text{Acid}] = \frac{(a-b)s}{(a+b)}$$

By Henderson equation

$$\text{pH} = \text{pK}_a + \log \frac{[\text{Salt}]}{[\text{Acid}]} = \text{pK}_a + \log \frac{b \times \cancel{s(a+b)}}{\cancel{(a+b)}(a-b)s}$$

$$\text{pH} = \text{pK}_a + \log \frac{b}{(a-b)}$$

$$\text{pH} = \text{pK}_a + 2.303 \ln \frac{b}{(a-b)} \quad \ln = \log_e$$

$$\frac{d(\text{pH})}{db} = 2.303 \frac{\cancel{(a-b)}}{b} \left[\frac{\cancel{(a-b)} \cdot 1 + b}{(a-b)^2} \right]$$

$$\frac{d(\text{pH})}{db} = 2.303 \frac{a}{b(a-b)}$$

$$\boxed{\beta = \frac{db}{d(\text{pH})} = \frac{1}{2.303} \frac{b(a-b)}{a}}$$

$$\frac{d\beta}{db} = \frac{1}{2.303} \cdot [b \times -1 + (a-b) \cdot 1]$$

$$\frac{d\beta}{db} = \frac{1}{2.303} = \frac{(a-2b)}{a}$$

$$\text{If } b = \frac{a}{2}, \frac{d\beta}{db} = 0$$

$$\frac{d^2\beta}{db^2} = (-) \text{ ve i.e. } b = \frac{a}{2} \text{ it is the condition of maxima.}$$

Conclusion : β is maximum at $b = \frac{a}{2}$. i.e for any buffer, buffer capacity (β) is maximum at half neutralization point.

$$\text{So, } \beta_{\max} = \frac{1}{2.303} \times \frac{a^2}{4a} = \frac{1}{2.303} \frac{a}{4}$$

$$\boxed{\beta_{\max} = \frac{1}{2.303} \frac{a}{4}}$$

Q1. 100 cc $\left(\frac{N}{10}\right)$ $\text{CH}_3\text{COOH} + 50 \text{ cc } \left(\frac{N}{10}\right)$ $\text{NaOH} \Rightarrow \text{pH ?}$ & comment on its Buffer capacity.

$$\text{pH} = 4.76 + \log \frac{\frac{50 \times \frac{1}{10}}{150}}{\frac{50 \times \frac{1}{10}}{150}}$$

$$\boxed{\text{pH} = 4.76} \text{ max } \beta$$